

THE VILLAGE INTERNATIONAL SCHOOL

RECAP ACTIVITY – SETS

1. Write the set $A = \{1, 4, 9, 16, 25, \dots\}$ in set-builder form.
2. Let $A = \{1, 2, 3, 4, 5, 6\}$. Insert the appropriate symbol \in or \notin in the blank spaces:
(i) $5 \dots A$ (ii) $8 \dots A$ (iii) $0 \dots A$
3. Write the following sets in roster form:
(i) $A = \{x : x \text{ is an integer and } -3 \leq x < 7\}$
(ii) $B = \{x : x \text{ is a natural number less than } 6\}$
(iii) $C = \{x : x \text{ is a two-digit natural number such that the sum of its digits is } 8\}$
4. Which of the following are examples of the null set
(i) Set of odd natural numbers divisible by 2
(ii) Set of even prime numbers
(iii) $\{x : x \text{ is a natural numbers, } x < 5 \text{ and } x > 7\}$
5. Write down all the subsets of the following sets (i) $\{a\}$ (ii) $\{a, b\}$
6. Write the following as intervals :
(i) $\{x : x \in \mathbb{R}, -4 < x \leq 6\}$
(ii) $\{x : x \in \mathbb{R}, -12 < x < -10\}$
(iii) $\{x : x \in \mathbb{R}, 0 \leq x < 7\}$
(iv) $\{x : x \in \mathbb{R}, 3 \leq x \leq 4\}$
7. Write the following intervals in set-builder form : (i) $(-3, 0)$ (ii) $[6, 12]$
8. Find the union of each of the following pairs of sets :
(i) $A = \{x : x \text{ is a natural number and multiple of } 3\}$ $B = \{x : x \text{ is a natural number less than } 6\}$

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9. If $A = \{x : x \text{ is a natural number}\}$, $B = \{x : x \text{ is an even natural number}\}$, $C = \{x : x \text{ is an odd natural number}\}$ and $D = \{x : x \text{ is a prime number}\}$, find (i) $A \cap B$ (ii) $A \cap C$ (iii) $A \cap D$
10. Which of the following pairs of sets are disjoint
- (i) $\{1, 2, 3, 4\}$ and $\{x : x \text{ is a natural number and } 4 \leq x \leq 6\}$
- (ii) $\{a, e, i, o, u\}$ and $\{c, d, e, f\}$
11. If $A = \{3, 6, 9, 12, 15, 18, 21\}$, $B = \{4, 8, 12, 16, 20\}$, $C = \{2, 4, 6, 8, 10, 12, 14, 16\}$, $D = \{5, 10, 15, 20\}$; find (i) $A - B$ (ii) $A - C$ (iii) $A - D$ (iv) $B - A$
12. Let $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$, $A = \{1, 2, 3, 4\}$, $B = \{2, 4, 6, 8\}$ and $C = \{3, 4, 5, 6\}$. Find (i) A' (ii) B' (iii) $(A \cup C)'$ (iv) $(A \cup B)'$ (v) (A')
13. If $A = \{x : x \text{ is a natural number}\}$, $B = \{x : x \text{ is an even natural number}\}$, $C = \{x : x \text{ is an odd natural number}\}$ and $D = \{x : x \text{ is a prime number}\}$, find (i) $A \cap B$ (ii) $A \cap C$ (iii) $A \cap D$
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16. Let $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$, $A = \{1, 2, 3, 4\}$, $B = \{2, 4, 6, 8\}$ and $C = \{3, 4, 5, 6\}$. Find (i) A' (ii) B' (iii) $(A \cup C)'$ (iv) $(A \cup B)'$ (v) (A')

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RECAP ACTIVITY – RELATIONS

1. If $(x + 1, y - 2) = (3, 1)$, find the values of x and y
2. If $P = \{a, b, c\}$ and $Q = \{r\}$, form the sets $P \times Q$ and $Q \times P$.
3. If the set A has 3 elements and the set $B = \{3, 4, 5\}$, then find the number of elements in $(A \times B)$.
4. Let A and B be two sets such that $n(A) = 3$ and $n(B) = 2$. If $(x, 1)$, $(y, 2)$, $(z, 1)$ are in $A \times B$, find A and B , where x , y and z are distinct elements.
5. Let $A = \{1, 2, 3, 4, 5, 6\}$. Define a relation R from A to A by $R = \{(x, y) : y = x + 1\}$ (i) Depict this relation using an arrow diagram. (ii) Write down the domain, codomain and range of R .
6. Determine the domain and range of the relation R defined by $R = \{(x, x + 5) : x \in \{0, 1, 2, 3, 4, 5\}\}$.
7. Let $A = \{x, y, z\}$ and $B = \{1, 2\}$. Find the number of relations from A to B .
8. If $A = \{1, 4, 8, 9\}$ and $B = \{1, 2, -1, -2, -3, 3, 5\}$ and R is a relation from set A to set B $\{(x, y) : x = y^2\}$. Write R in roster form.

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RECAP ACTIVITY – SEQUENCES AND SERIES

1. Find the next term of the sequence
2,8,32,128,.....
2. Find the indicated terms in each of the sequences in whose nth terms are:
(i) $a_n = 4n - 3$; a_{12} , a_{15}
(ii) $a_n = \frac{n^2}{2}$; a_5 , a_7
3. Write the first five terms of each of the sequences and obtain the corresponding series:
(i) $a_1 = 3, a_n = 3a_{n-1} + 2$ for all $n > 1$
(ii) $a_1 = -1, a_n = \frac{a_{n-1}}{n}$, $n \geq 2$
4. Find the 7th term of the sequence -
5,-2,1,4,.....85
5. The sums of n terms of two arithmetic progressions are in the ratio $3n+8: 7n+15$. Find the ratio of their 12th terms.
6. Find the sum of the following series. (a) $4 + 7 + 10 + \dots$ to 100 terms (b) $1 + 4^3 + 5^3 + 2 + \dots$ to 19 term
7. The third term of a G.P. is 12. Find the product of its first five terms.
8. Find the 20th and nth terms of the
G.P. $\frac{5}{2}, \frac{5}{4}, \frac{5}{8} \dots \dots$

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9. A manufacturer reckons that the value of a machine, which costs him Rs. 56200, will depreciate each year by 20%. Find the estimated value at the end of 3 years.
10. Insert two numbers between 3 and 81 so that the resulting sequence is G.P.
11. If AM and GM of two positive numbers x and y are 13 and 12 respectively, find the numbers.
12. Find the sum of the G.P.
1,3,9,27,.....to 7 terms

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RECAP ACTIVITY – PERMUTATIONS AND COMBINATIONS

1. Evaluate (i) $5!$ (ii) $7!$ (iii) $7! - 5!$
2. Compute (1) $\frac{7!}{5!}$ (2) $\frac{12!}{10! 2!}$
3. Compute $\frac{8!}{6! \times 2!}$
4. Express the following in factorial notation. (i) $6 \times 7 \times 8 \times 9$
(ii) $4 \times 5 \times 6 \times 7 \times 8$
5. How many 3-digit numbers can be formed from the digits 1, 2, 3, 4 and 5 assuming that
(i) repetition of the digits is allowed?
(ii) repetition of the digits is not allowed?
6. How many 3-digit even numbers can be formed from the digits 1, 2, 3, 4, 5, 6 if the digits can be repeated?
7. How many 4-letter code can be formed using the first 10 letters of the English alphabet, if no letter can be repeated?
8. How many 5-digit telephone numbers can be constructed using the digits 0 to 9 if each number starts with 67 and no digit appears more than once?
9. Find the value of n such that ${}^n P_4 = 20 {}^n P_2$, $n > 3$
How many 3-digit numbers can be formed by using the digits 1 to 9 if no digit is repeated? 2. How many 4-digit numbers are there with no digit repeated? 3. How many 3-digit even numbers can be made using the digits 1, 2, 3, 4, 6, 7, if no digit is repeated? 4. Find the

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number of 4-digit numbers that can be formed using the digits 1, 2, 3, 4, 5 if no digit is repeated. How many of these will be even? 5.

From a committee of 8 persons, in how many ways can we choose a chairman and a vice chairman assuming one person can not hold more than one position?

10. If $nC8 = nC2$, find $nC2$.
11. In how many ways can a team of 3 boys and 3 girls be selected from 5 boys and 4 girls?
12. Find the number of ways of selecting 9 balls from 6 red balls, 5 white balls and 5 blue balls if each selection consists of 3 balls of each colour.
13. Determine the number of 5 card combinations out of a deck of 52 cards if there is exactly one ace in each combination

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